

## A BRIEF DESCRIPTION OF THREE TUNING SYSTEMS

### EQUAL TEMPERAMENT

With equal temperament, all intervals are equally out of tune. It is often argued that equal temperament can be offensive to musicians with keen ears. The space of an octave is divided into twelve equal parts called semitones or half steps, with each tone equal distance from the next (octave equivalence). These tones do not exactly agree with the frequencies of pitch found in the overtone series. The tones are tempered or adjusted; the tuning system is called equal temperament, since the twelve half steps are equal in size. The intervals in equal temperament are fixed as a piano keyboard.

### PYTHAGOREAN SCALE

Pythagoras, a Greek mathematician and philosopher (582-500 B.C.), is thought to have made certain acoustic experiments with a vibrating string called the monochord. By using two monochords, he performed an experiment in which the string of one monochord was successively shortened by one-half (raising the pitch an octave), and the string of the other was shortened each time by two-thirds (raising the pitch a fifth). After seven octaves and twelve fifths, Pythagoras discovered that the B# from the second monochord was not exactly the same as the C produced by the first monochord, but slightly higher. This small discrepancy is called the Pythagorean comma. The tuning systems differ in the manner in which this comma is handled.

The Pythagorean scale derives all tones from the interval of the pure fifth ( $3/2$ ) as it occurs in the overtone series. This tuning system produces a sharper, brighter sound and is particularly good for barbershop harmony.

### JUST INTONATION

This system attempts to improve upon the deficiencies of the Pythagorean scale by basing the calculations on both pure fifths ( $3/2$ ) and pure thirds ( $5/4$ ). The just intonation scale multiplies its difficulties as soon as chromatic tones are introduced. Sharps are actually lower in pitch than the flats. Some musicians love just temperament dearly. One musician had a harmonium just tuned in the key of C. It sounded excellent in C, but dreadful when played in any other key.

COMPARISON OF SELECTED FREQUENCIES USING THREE TUNING SYSTEMS

| Scale Tone     | Interval From Root | Equal-Temperament Scale |          | Pythagorean Scale |          |          | Just Intonation (Overtone Series) Zarbino Scale |       |          |
|----------------|--------------------|-------------------------|----------|-------------------|----------|----------|---|-------|----------|
|                |                    | Log Cents               | Freq. Hz | Log Cents         | Ratio    | Freq. Hz | Log Cents                                       | Ratio | Freq. Hz |
| A              | Unison             | 0                       | 220.000  | 0                 | 1:1      | 220.000  | 0   | 1:1   | 220.000  |
| A# / Bb        | Min. 2             | 100                     | 233.082  | 90                | 256:243  | 231.7695 | 112   | 16:15 | 234.667  |
| B              | Maj. 2             | 200                     | 246.942  | 204               | 9:8      | 247.500  | 204   | 9:8   | 247.500  |
| C <sup>i</sup> | Min. 3             | 300                     | 261.626  | 294               | 32:27    | 260.7407 | 315   | 6:5   | 264.000  |
| C# / Db        | Maj. 3             | 400                     | 277.183  | 408               | 81:64    | 278.4375 | 385   | 5:4   | 275.000  |
| D              | Perf. 4            | 500                     | 293.665  | 498               | 4:3      | 293.333  | 498   | 4:3   | 293.333  |
| D# / Eb        | Aug. 4 /<br>Dim. 5 | 600                     | 311.127  | 612               | 729:512  | 313.242  | 590   | 45:32 | 309.375  |
|                |                    | 600                     | 311.127  | 588               | 1024:729 | 309.026  | 610   | 64:45 | 312.889  |
| E              | Perf. 5            | 700                     | 329.628  | 702               | 3:2      | 330.000  | 702   | 3:2   | 330.000  |
| F              | Min. 6             | 800                     | 349.228  | 792               | 128:81   | 347.6543 | 814   | 8:5   | 352.000  |
| F# / Gb        | Maj. 6             | 900                     | 369.994  | 906               | 27:16    | 371.250  | 884   | 5:3   | 366.667  |
| G              | Min. 7             | 1000                    | 391.995  | 996               | 16:9     | 391.111  | 996   | 16:9  | 391.111  |
| G# / Ab        | Maj. 7             | 1100                    | 415.305  | 1110              | 243:128  | 417.6562 | 1088  | 15:8  | 412.500  |
| A              | Octave             | 1200                    | 440.000  | 1200              | 2:1      | 440.000  | 1200  | 2:1   | 440.000  |

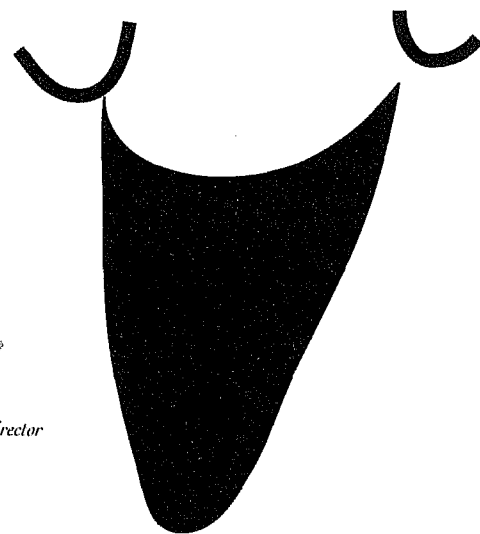
# Pythagorean Tuning

| Scale Position         | DO        | SOL       | RE'       | LA        | MI        | TI         | FI         | DI         | SI         | RI         | LI         |            | SE'        | RA         | LE'       | ME'       | TE'       | FA        |    |
|------------------------|-----------|-----------|-----------|-----------|-----------|------------|------------|------------|------------|------------|------------|------------|------------|------------|-----------|-----------|-----------|-----------|----|
| <b>KEY</b>             | <b>0</b>  | <b>+2</b> | <b>+4</b> | <b>+6</b> | <b>+8</b> | <b>+10</b> | <b>+12</b> | <b>+14</b> | <b>+16</b> | <b>+18</b> | <b>+20</b> | <b>-14</b> | <b>-12</b> | <b>-10</b> | <b>-8</b> | <b>-6</b> | <b>-4</b> | <b>-2</b> |    |
|                        | <b>C</b>  | C         | G         | D         | A         | E          | B          | F#         | C#         | G#         | D#         | A#         | Cb         | Gb         | Db        | Ab        | Eb        | Bb        | F  |
|                        | <b>G</b>  | G         | D         | A         | E         | B          | F#         | C#         | G#         | D#         | A#         | E#         | Gb         | Db         | Ab        | Eb        | Bb        | F         | C  |
|                        | <b>D</b>  | D         | A         | E         | B         | F#         | C#         | G#         | D#         | A#         | E#         | B#         | Db         | Ab         | Eb        | Bb        | F         | C         | G  |
|                        | <b>A</b>  | A         | E         | B         | F#        | C#         | G#         | D#         | A#         | E#         | B#         | F##        | Ab         | Eb         | Bb        | F         | C         | G         | D  |
|                        | <b>E</b>  | E         | B         | F#        | C#        | G#         | D#         | A#         | E#         | B#         | F##        | C##        | Eb         | Bb         | F         | C         | G         | D         | A  |
|                        |           |           |           |           |           |            |            |            |            |            |            |            |            |            |           |           |           |           |    |
| <b>ENHARMONIC KEYS</b> | <b>B</b>  | B         | F#        | C#        | G#        | D#         | A#         | E#         | B#         | F##        | C##        | G##        | Bb         | F          | C         | G         | D         | A         | E  |
|                        | <b>Cb</b> | Cb        | Gb        | Db        | Ab        | Eb         | Bb         | F          | C          | G          | D          | A          | Cbb        | Gbb        | Dbb       | Abb       | Ebb       | Bbb       | Fb |
|                        |           | 0         | +2        | +4        | +6        | +8         | +10        | +12        | +14        | +16        | +18        | +20        | -14        | -12        | -10       | -8        | -6        | -4        | -2 |
|                        | <b>F#</b> | F#        | C#        | G#        | D#        | A#         | E#         | B#         | F##        | C##        | G##        | D##        | F          | C          | G         | D         | A         | E         | B  |
|                        | <b>Gb</b> | Gb        | Db        | Ab        | Eb        | Bb         | F          | C          | G          | D          | A          | E          | Gbb        | Dbb        | Abb       | Ebb       | Bbb       | Fb        | Cb |
|                        |           |           |           |           |           |            |            |            |            |            |            |            |            |            |           |           |           |           |    |
|                        | <b>C#</b> | C#        | G#        | D#        | A#        | E#         | B#         | F##        | C##        | G##        | D##        | A##        | C          | G          | D         | A         | E         | B         | F# |
|                        | <b>Db</b> | Db        | Ab        | Eb        | Bb        | F          | C          | G          | D          | A          | E          | B          | C          | G          | D         | A         | E         | B         | F# |
|                        | <b>Ab</b> | Ab        | Eb        | Bb        | F         | C          | G          | D          | A          | E          | B          | F#         | Abb        | Ebb        | Bbb       | Fb        | Cb        | Gb        | Db |
|                        | <b>Eb</b> | Eb        | Bb        | F         | C         | G          | D          | A          | E          | B          | F#         | C#         | Ebb        | Bbb        | Fb        | Cb        | Gb        | Db        | Ab |
|                        | <b>Bb</b> | Bb        | F         | C         | G         | D          | A          | E          | B          | F#         | C#         | G#         | Bbb        | Fb         | Cb        | Gb        | Db        | Ab        | Eb |
|                        | <b>F</b>  | F         | C         | G         | D         | A          | E          | B          | F#         | C#         | G#         | D#         | Fb         | Cb         | Gb        | Db        | Ab        | Eb        | Bb |
|                        |           |           |           |           |           |            |            |            |            |            |            |            |            |            |           |           |           |           |    |
| <b>KEY</b>             | <b>0</b>  | <b>+2</b> | <b>+4</b> | <b>+6</b> | <b>+8</b> | <b>+10</b> | <b>+12</b> | <b>+14</b> | <b>+16</b> | <b>+18</b> | <b>+20</b> | <b>-14</b> | <b>-12</b> | <b>-10</b> | <b>-8</b> | <b>-6</b> | <b>-4</b> | <b>-2</b> |    |
| Scale Position         | DO        | SOL       | RE'       | LA        | MI        | TI         | FI         | DI         | SI         | RI         | LI         |            | SE'        | RA         | LE'       | ME'       | TE'       | FA        |    |

# Tuning Chart

| Key<br>Signature | Key            | +8 mi          | +6 la          | +10 ti         |
|------------------|----------------|----------------|----------------|----------------|
| —                | C              | E              | A              | B              |
| 1 <sub>b</sub>   | F              | A              | D              | E              |
| 2 <sub>b</sub>   | B <sub>b</sub> | D              | G              | A              |
| 3 <sub>b</sub>   | E <sub>b</sub> | G              | C              | D              |
| 4 <sub>b</sub>   | A <sub>b</sub> | C              | F              | G              |
| 5 <sub>b</sub>   | D <sub>b</sub> | F              | B <sub>b</sub> | C              |
| 6 <sub>b</sub>   | G <sub>b</sub> | B <sub>b</sub> | E <sub>b</sub> | F              |
| 7 <sub>b</sub>   | C <sub>b</sub> | E <sub>b</sub> | A <sub>b</sub> | B <sub>b</sub> |
| 1 <sub>#</sub>   | G              | B              | E              | F <sub>#</sub> |
| 2 <sub>#</sub>   | D              | F <sub>#</sub> | B              | C <sub>#</sub> |
| 3 <sub>#</sub>   | A              | C <sub>#</sub> | F <sub>#</sub> | G <sub>#</sub> |
| 4 <sub>#</sub>   | E              | G <sub>#</sub> | C <sub>#</sub> | D <sub>#</sub> |
| 5 <sub>#</sub>   | B              | D <sub>#</sub> | G <sub>#</sub> | A <sub>#</sub> |
| 6 <sub>#</sub>   | F <sub>#</sub> | A <sub>#</sub> | D <sub>#</sub> | E <sub>#</sub> |
| 7 <sub>#</sub>   | C <sub>#</sub> | E <sub>#</sub> | A <sub>#</sub> | B <sub>#</sub> |

# My Director's Always Saying...



by Lorraine Barrows (#25, Chapter-at-Large), headquarters' Director of Education, IES Planning Committee, Certified Director

## “Pythagorean Tuning”

One Education Direction Committee member was heard to say, “How will Pythagoras change my life? And is he busy Saturday night?”

Simply put, Pythagoras could make your highs higher, your lows lower, and you'd be satisfied! Though many different

scales exist, all with different advantages, Pythagorean tuning alters certain scale steps ever so slightly to accommodate the “lock and ring” of common barbershop chords. In its simplest form, the 3rd, 6th, 7th, and # 4th steps of the scale are the notes most noticeably raised (or sung a lit-

tle bit sharp). In the key of C, we would raise the E, A, B, and F# when it is written in as an accidental. (Although some scale steps can be used to slightly flatten, most directors don't say anything about them to keep chorus members from flattening any more than they do on their own!)

## Women of Note/Directors of Note

Sweet Adelines International recognizes the following international program participants on their recent advancements.

### *Director Certification Program*

#### **Advanced to Master Director:**

Christine Ferguson, #1, Royal River Chorus  
LeAnn Hazlett, #2, Spirit of Detroit Chorus  
Becki Hine, #23, Song of Atlanta Chorus  
Molly Huffman, #4, Capital City Chorus  
Ann Jarchow, #3, Grand Rapids Chorus  
Bev Miller, #4, Capital City Chorus  
Anna Nyberg, #32, Stockholm City Chorus  
Sandy Robinson, #26, Lions Gate Chorus

#### **Advanced to Certified Director:**

Fay Baker, #34, Chapter-at-Large  
Heather Bartlett, #31, City of Roses Chorus  
Sally Beck, #25, Sooner Sensations Chorus

Jerri Beyrodt, #24, Mountain River Harmony Chorus  
Margaret Butt, #1, North Shore Chorus  
Judith Hunt, #31, Surrey Harmony Chorus  
Jeanette Hupe, #7, Wamego Dutch Mill Chorus  
Jenny Lawson, #31, Surrey Harmony Chorus  
Wendy Lenihan, #15, Eastern Suffolk Chorus  
Barbara Letcher, #35, Greater Auckland Chorus  
Mike McGee, #11, Agoura Hills Harmony Chorus  
Christien Oberholster, #35, Whangarei Harmony Chorus  
Carol Reed, #16, St. Lawrence Chorus  
Peggy Staats, #11, Channelaire Chorus  
Carol Stenstrom, #14, Southern Harmony Chorus  
Gwen Topp, #31, Aberdeen Chorus  
Nancy Watson, #16, Greater Kingston Chorus

"Lies My Music Teacher Told Me"--Gerald Eskelin

(Music Theory for Grown ups)

Very entertaining, written for the musician, great insights on relative pitch, tuning, lock and ring, methods of teaching pitch and intervals, use of Pythagorean Tuning and rhythm teaching that illustrate ideals of a cappella singing. A book I wish I'd read years ago! Great discussion of the overtone series in a fun, entertaining presentation. Great applications to chorus and quartet singing. Full of memorable quotes.